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10ES36

Third Semester B.E. Degree Examination, Dec.2017/Jan.2018
Field Theory

Time: 3 hrs.

Max. Marks:100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART – A

- 1
 - a. State and prove gauss law for electrostatics. (06 Marks)
 - b. If $E = (-8xy\hat{a}_x - 4x^2\hat{a}_y + \hat{a}_z)$ V/m. Find the work done in carrying a 6 C charge from A(1, 8, 5) to B(2, 18, 6) along the path $y = 3x + 2$, $z = x + 4$ (06 Marks)
 - c. Four point charges each 20 μC are at A(4, 0, 0), B(-4, 0, 0), C(0, 4, 0), D(0, -4, 0) respectively. Find the force on a 200 μC point charge at (0, 0, 3). (08 Marks)
- 2
 - a. Derive an equation for divergence of flux density in differential form, and hence explain Gauss divergence theorem. (08 Marks)
 - b. A 15 nC point charge is at the origin in free space. Calculate v_1 if point P is located at (2, -3, -1). Also calculate v_1 at P if $v = 0$ at (6, 5, 4) (06 Marks)
 - c. Deduce an expression for energy and energy density in an electro static field. (06 Marks)
- 3
 - a. Using Poisson's equation, obtain the expression for junction potential in a p-n junction. (08 Marks)
 - b. Derive Laplace's equation and hence write the expression for Laplacian of V in cylindrical and spherical co-ordinates. (06 Marks)
 - c. Find E at P(3, 1, 2) for the field of two co-axial conducting cylinders. $V = 50$ V at $r = 2$ m, $V = 20$ V at $r = 3$ m. (06 Marks)
- 4
 - a. Derive an expression for magnetic flux density (\vec{B}) due to straight conductor of finite length. (06 Marks)
 - b. If \vec{H} in a region is $2x\hat{a}_y + (3y - 2)\hat{a}_z$, find the current density at the origin. (06 Marks)
 - c. Given the magnetic field $\vec{H} = 2r^2(z+1)\sin\phi\hat{a}_\phi$, verify Stoke's theorem for the portion of cylindrical surface defined by $r = 2$, $\frac{\pi}{4} < \phi < \frac{\pi}{2}$, $1 < z < 1.5$. (08 Marks)

PART – B

- 5
 - a. Find the magnetic flux density due to long current carrying conductor using vector magnetic potential. (08 Marks)
 - b. Derive the expression for boundary conditions, if the field lines are tangent and normal to the boundary line between two media's in static magnetic field. (06 Marks)
 - c. A solenoid with air core has 2000 turns and a length of 500 mm, core radius 40 mm. Find its inductance. (06 Marks)

- 6 a. Derive the modification of Ampere's circuit law to suit for time varying conditions. (06 Marks)
- b. Explain Maxwell's equations in point and integral form. Establish relationship between conduction current density and displacement current density for the given field $E = E_0 \sin \omega t$ (08 Marks)
- c. Do the fields $E = E_m \sin x \sin t \hat{a}_y$ and $\vec{H} = \frac{E_m}{\mu} \cos x \cos t \hat{a}_z$. Satisfy Maxwell's equations. Verify. (06 Marks)
- 7 a. Derive an expression for electric and magnetic wave equations. (06 Marks)
- b. For an electromagnetic wave propagating in free space, show that $\frac{E}{H} = \eta$. (08 Marks)
- c. Find skin depth and surface resistance of copper conductor at 100 MHz having conductivity $\sigma = 5.8 \times 10^7 \text{ S/m}$ and $\mu_r = 100$. (06 Marks)
- 8 a. Explain the reflection of uniform plane wave with normal incidence at a plane dielectric boundary. (10 Marks)
- b. Write short notes on:
- Reflection co-efficient.
 - Standing wave ratio. (10 Marks)